Congruence

Two plane figures are congruent if one fits exactly on the other. They must be the same size and the same shape.

Exercise 7

1. Identify pairs of congruent shapes below.



- 2. Triangle LMN is isosceles with LM = LN; X and Y are points on LM, LN respectively such that LX = LY. Prove that triangles LMY and LNX are congruent.
- 3. ABCD is a quadrilateral and a line through A parallel to BC meets DC at X. If $\widehat{D} = \widehat{C}$, prove that $\triangle ADX$ is isosceles.
- 4. In the diagram, N lies on a side of the square ABCD, AM and LC are perpendicular to DN. Prove that:
 (a) ADN = LCD
 (b) AM = LD



- 5. Points L and M on the side YZ of a triangle XYZ are drawn so that L is between Y and M. Given that XY = XZ and YXL = MXZ, prove that YL = MZ.
- 6. Squares AMNB and AOPC are drawn on the sides of triangle ABC, so that they lie outside the triangle. Prove that MC = OB.
- 7. In the diagram, LMN = ONM = 90°. P is the mid-point of MN, MN = 2ML and MN = NO. Prove that:
 (a) the triangles MNL and NOP are congruent
 (b) OPN = LNO
 (c) LQO = 90°



8. PQRS is a parallelogram in which the bisectors of the angles P and Q meet at X. Prove that the angle PXQ is a right angle.